

Designing Lunar Navigation Satellite Systems



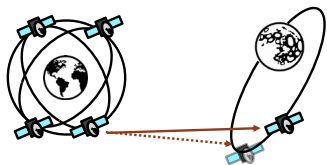
PROF. GRACE X. GAO



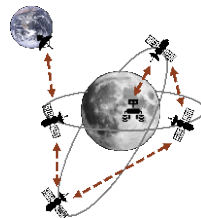
Designing Lunar Navigation Satellite Systems



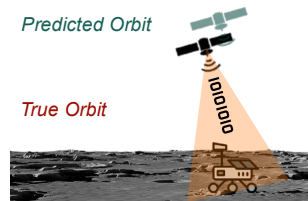
1. Using GNSS for Time and Orbit Determination



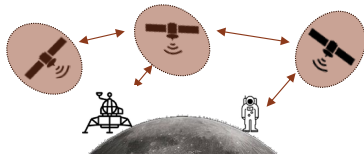
2. System Design and Tradeoff Studies



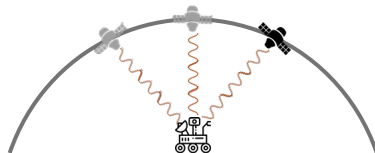
3. Ephemeris and Code Design



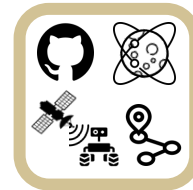
4. Using Crosslinks for Scheduling and Integrity



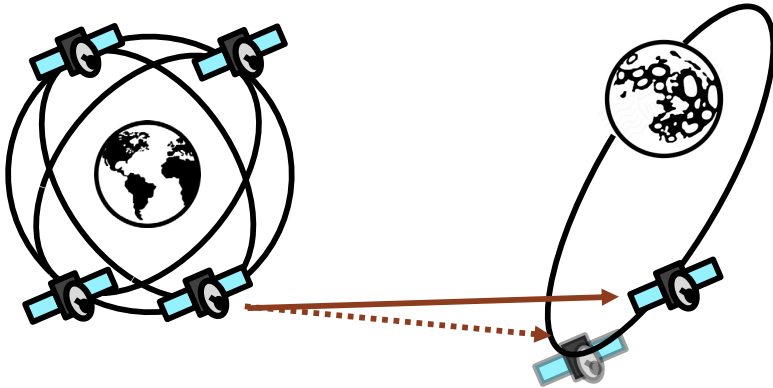
5. Intermediate step with 1-2 satellites



6. LuPNT: an Open-Source Simulator

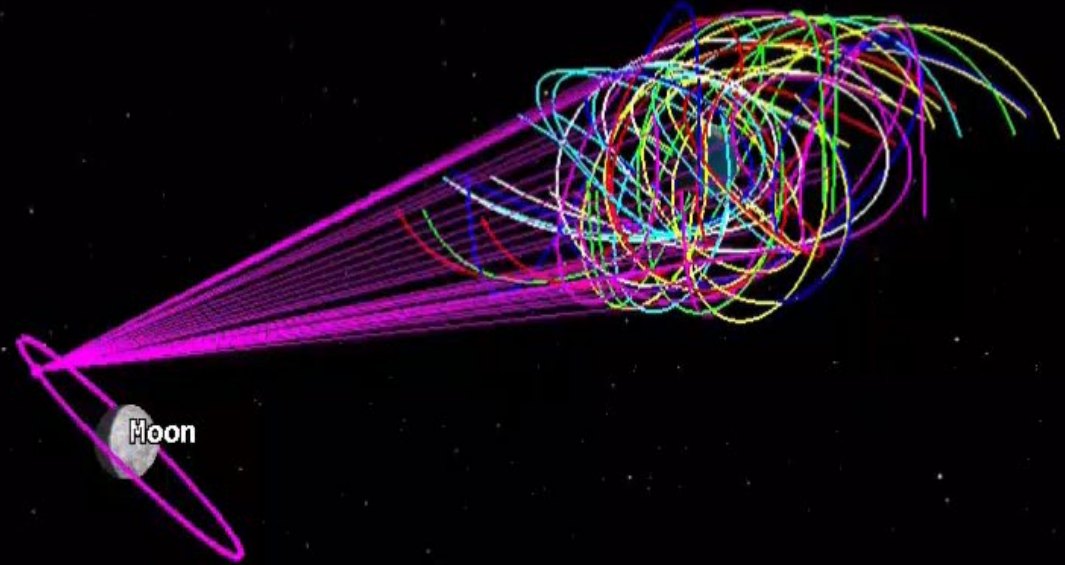


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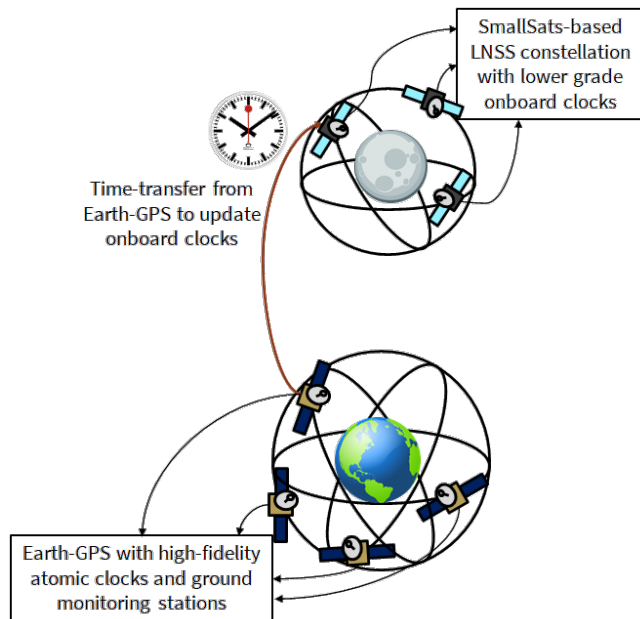
- Iiyama, Bhamidipati and Gao, ION Navigation Journal 2024
- Iiyama and Gao, ION GNSS+ 2023
- Iiyama, Bhamidipati and Gao, IEEE Aerospace Conf. 2023
- Iiyama, Bhamidipati and Gao, ION ITM 2023
- Bhamidipati, Mina and Gao, ION Navigation Journal 2022
- Bhamidipati, Mina, Sanchez and Gao, ION GNSS+ 2022
- Sanchez and Gao, ION GNSS+ 2022
- Bhamidipati, Iiyama, Mina and Gao, IEEE Aerospace Conf. 2022

Utilizing GNSS Signals

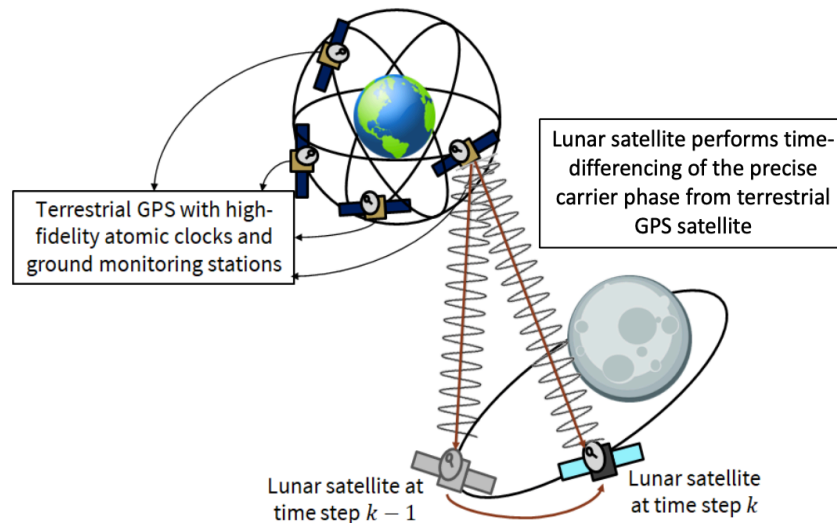


Utilizing GNSS Signals

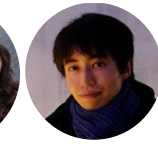
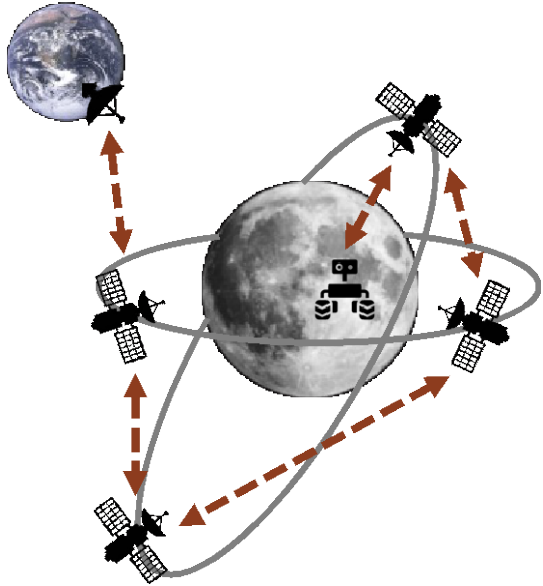
Lunar Satellite Clock Correction: Time-Transfer from GNSS



Orbital Determination: GNSS Time Differenced Carrier Phase (TDCP)



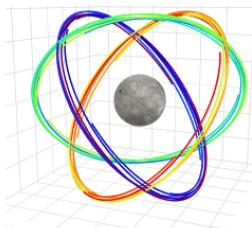
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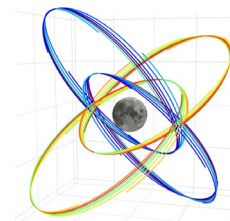
- Bhamidipati, Mina and Gao, ION Navigation Journal 2023
- Bhamidipati, Mina and Gao, ION Navigation Journal 2023 (2)
- Bhamidipati, Mina and Gao, ION Navigation Journal 2022
- Bhamidipati, Mina, Sanchez and Gao, ION GNSS+ 2022
- Sanchez and Gao, ION GNSS+ 2022
- Bhamidipati, Iiyama, Mina and Gao, IEEE Aerospace Conf. 2022
- Bhamidipati, Mina and Gao, ION ITM 2022
- Bhamidipati, Mina and Gao, ION GNSS+ 2021

Constellation Design for Full Coverage

We consider 2 types of symmetrical constellations



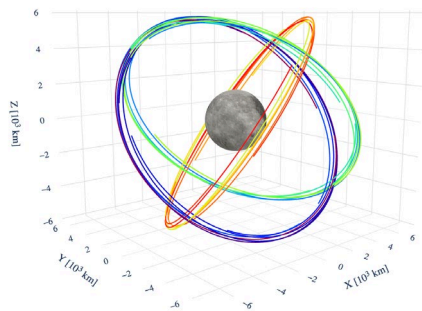
Walker
Constellation
(18 sats required)



ELFO
Constellation
(24 sats required)

Orbit Type	Circular	Elliptical
Stability	Moderate	Very Stable
Global coverage	Excellent	Moderate
Pole visibility	Moderate	Excellent

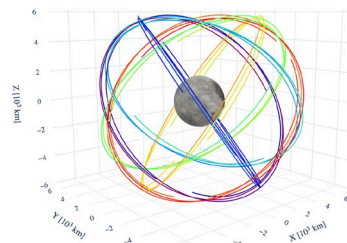
3-plane configuration (6 sats each)



Minimum altitude:
4300 - 4500 km

Best Inclination:
 ≈ 55 deg

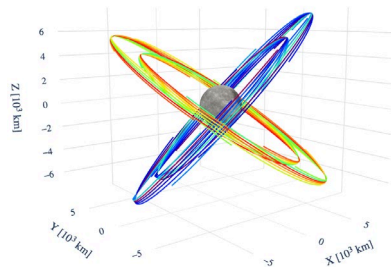
6-plane configuration (3 sats each)



Minimum altitude: ———
6500 - 6700 km

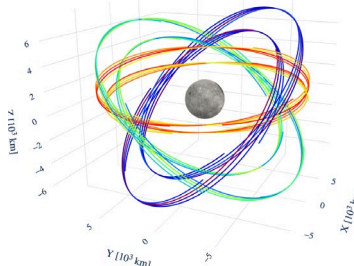
Best Inclination:
 ≈ 55 deg

4-plane configuration (6 sat each)



Minimum
semi-major axis:
8000 - 9000 km
Best Inclination:
40 deg

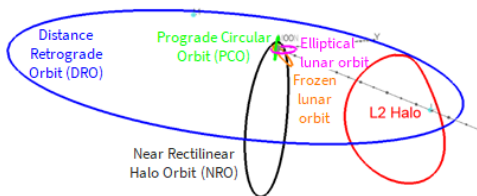
6-plane configuration (4 sat each)



Minimum
semi-major axis:
7000 - 8000 km
Best Inclination:
40 deg

Trade-off Studies and Case Studies

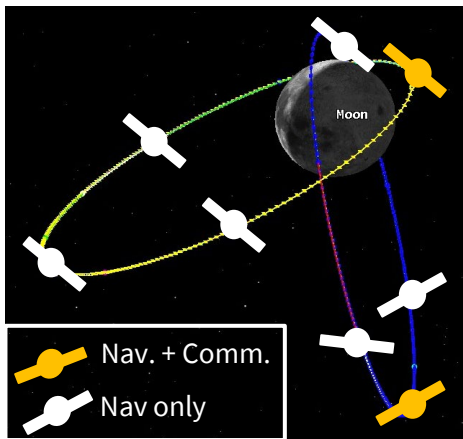
Orbit choices:



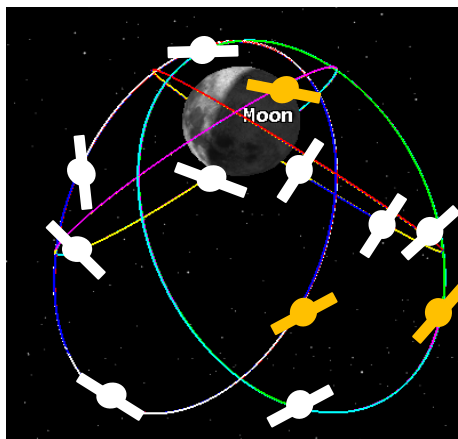
Clock choices:



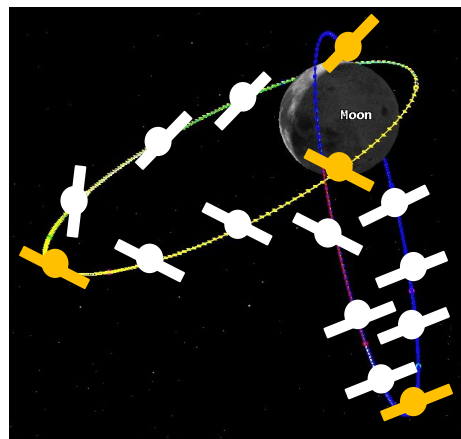
CASE-A: 6 nav-only SVs,
2 nav+comm SVs



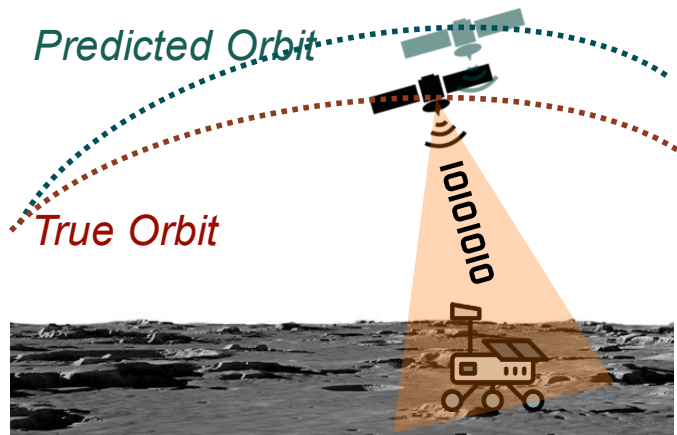
CASE-B: 9 nav-only SVs,
3 nav+comm SVs



CASE-C: 12 nav-only SVs,
4 nav+comm SVs



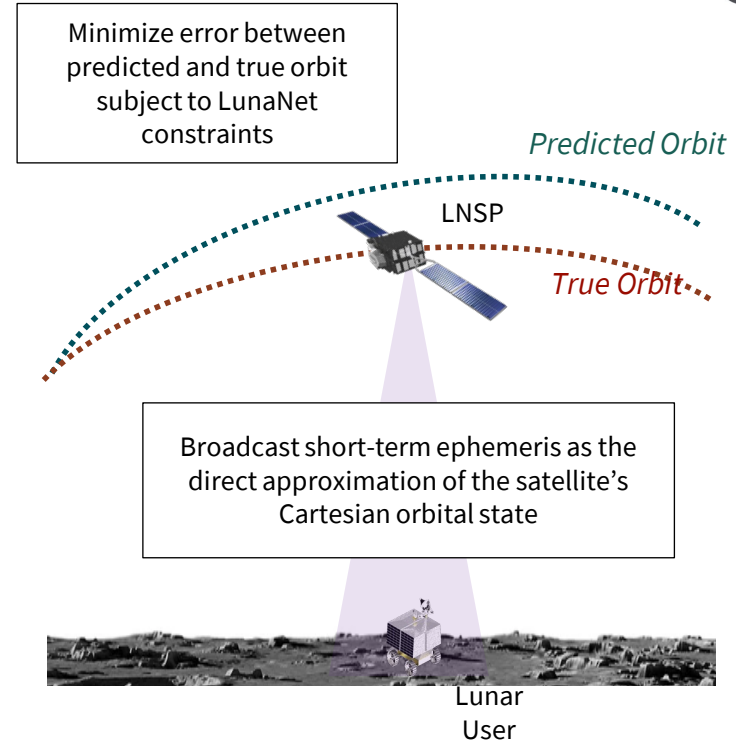
3. Ephemeris and Code Design



- Cortinovis, Iiyama and Gao, *ION Navigation Journal* 2024
- Cortinovis, Iiyama and Gao, *ION GNSS+ 2023*
- Yang, Mina, Boyd and Gao, *ION GNSS+ 2024*
- Yang, Mina and Gao, *EURASIP Journal on Advances in Signal Processing*, 2024
- Yang, Mina, and Gao, *ION ITM 2024*
- Yang, Mina, and Gao, *IEEE ICASSP 2023*
- Yang, Mina, and Gao, *ION GNSS+ 2023*
- Mina, Yang and Gao, *ION GNSS+ 2023*

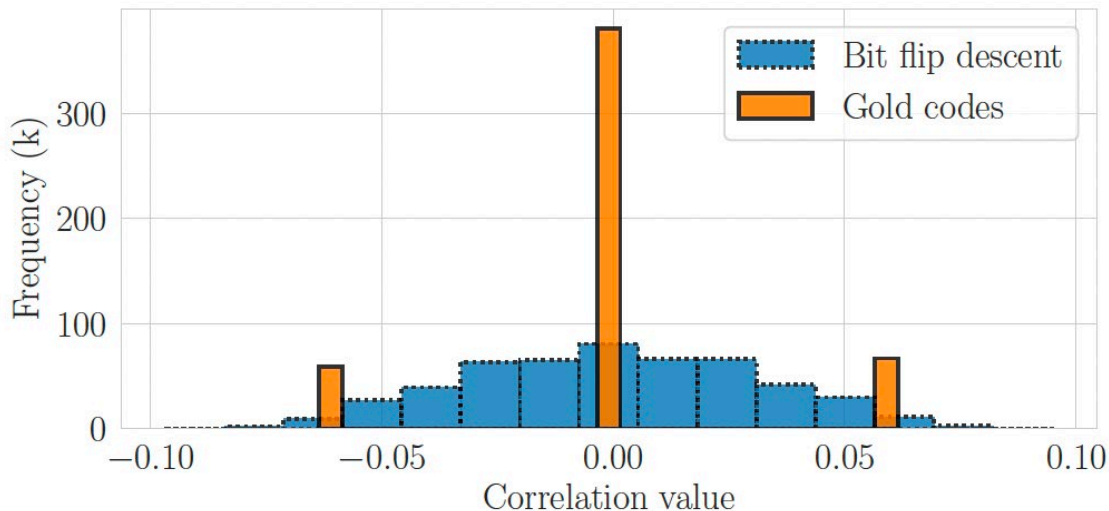
Ephemeris Design

- **Constrained convex optimization**
- **Cartesian-based model** vs Orbital Parameterization Model
- Tradeoff among **precision**, **duration**, and **broadcast data volume**
- Compliant parameterizations with Polynomial and Chebyshev models
- Decreased message length with Chebyshev model

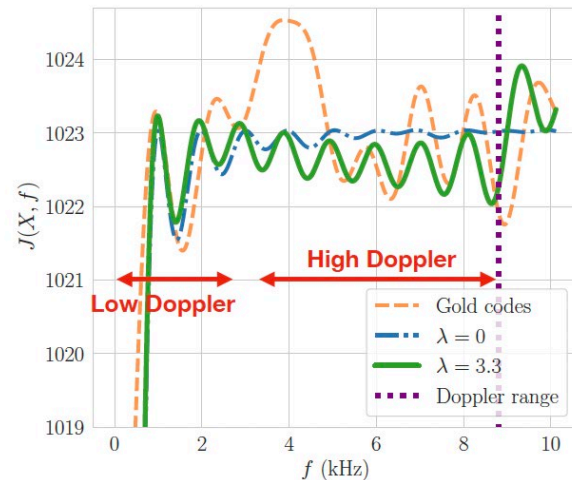


Pseudo-Random Noise (PRN) Code Design

Improved correlation properties

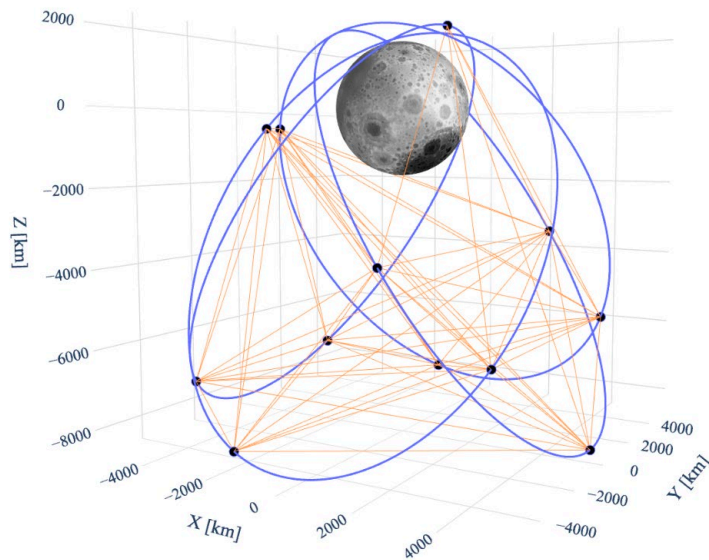


Considering Doppler effect



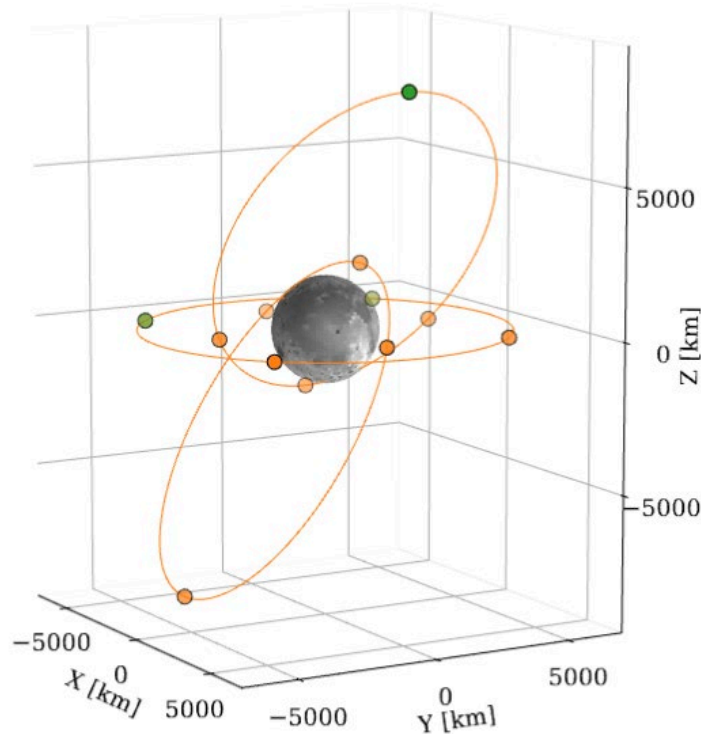
$$n = 31, T = 1023$$

4. Using Crosslinks for Scheduling and Integrity

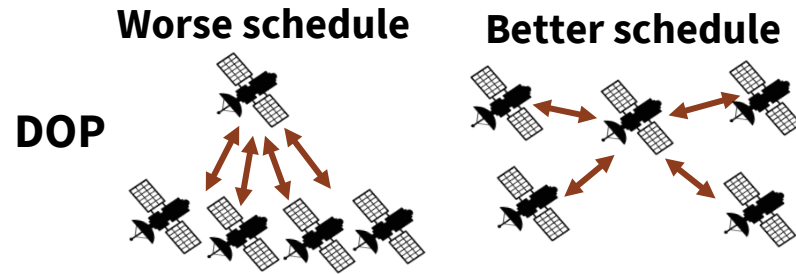


- Casadesus Vila and Gao, *ION GNSS+ 2024*
- Iiyama, Neamati and Gao, *ION GNSS+ 2024*
- Iiyama, Casadesus Vila and Gao, *IEEE Aerospace Conf. 2024*

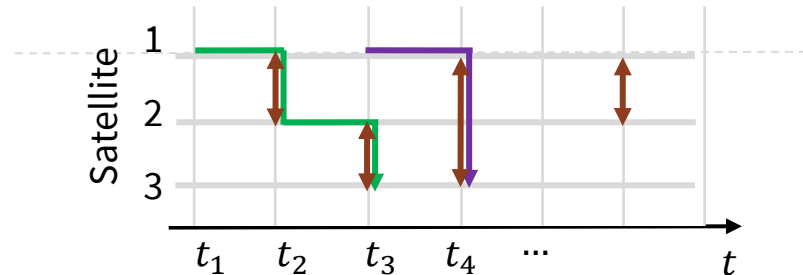
Crosslink Scheduling & Distributed PNT



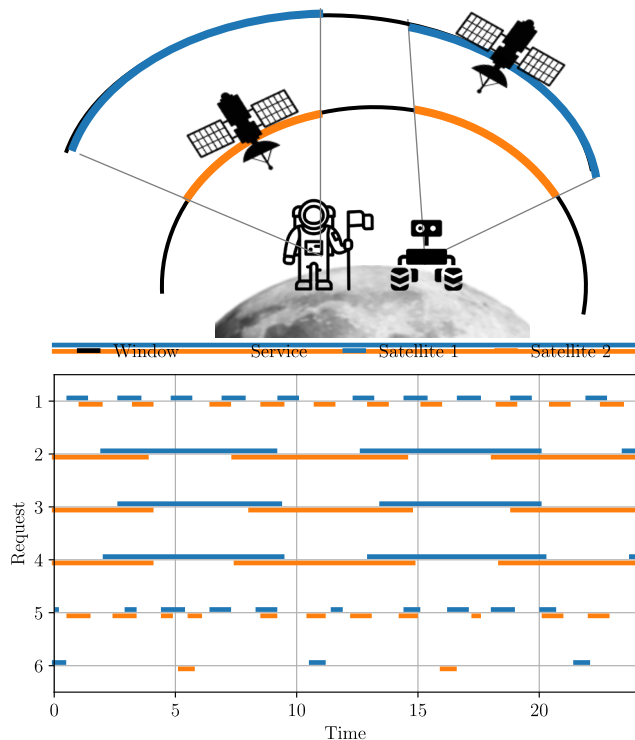
For Orbital Determination and Time Synchronization: (ODTS):



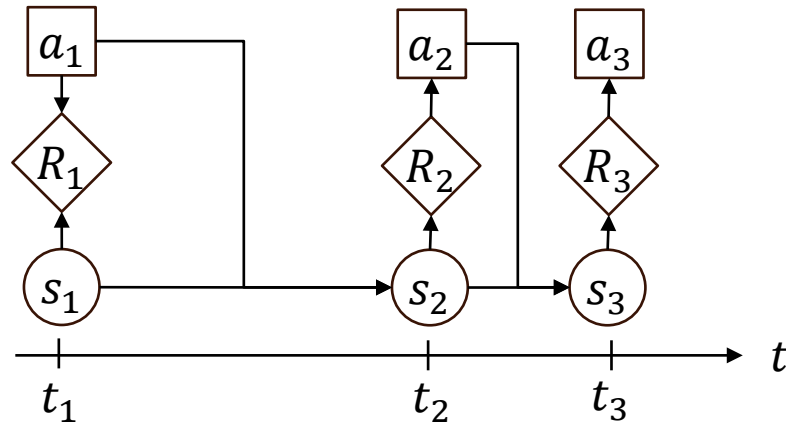
For communication:
Link schedule



Service Scheduling using Markov Design Processes



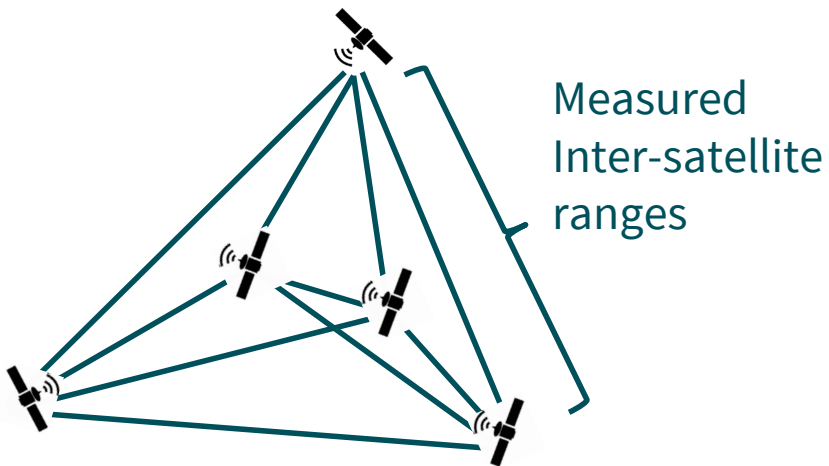
Semi-MDP (SMDP): non-uniform time step



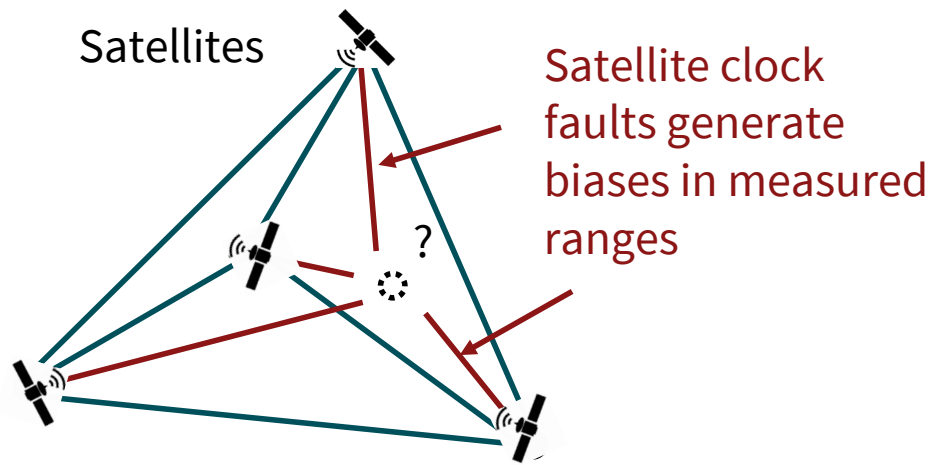
Fault Detection using Rigid Graphs

We propose an **onboard satellite fault detection** algorithm that uses a **rigid graphs** constructed from a set of **inter-satellite ranges**

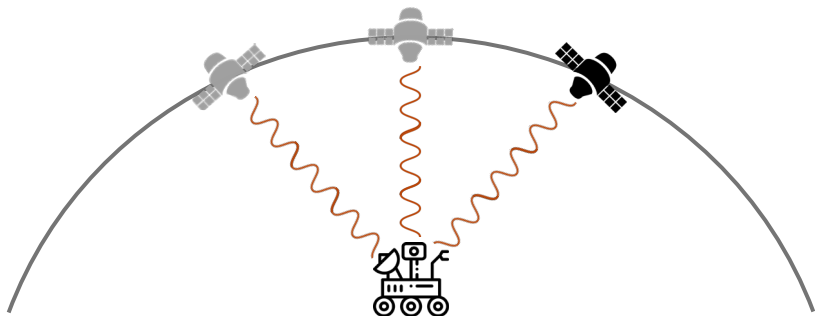
We construct a “rigid” graph, which cannot be deformed



We detect faults when the given set of ranges is not realizable in 3D space

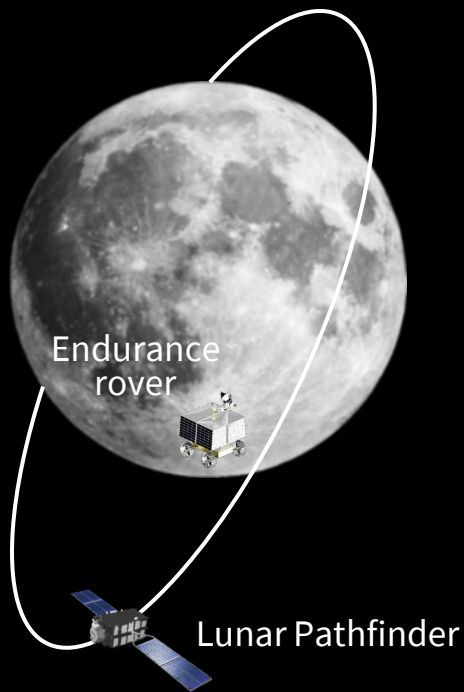


5. Intermediate step with 1-2 satellites



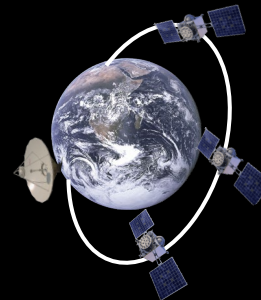
- Coimbra and Gao, *IEEE Aerospace Conf. 2025*
- Coimbra, Cortinovis, Mina and Gao, *ION GNSS+ 2024*
- Cortinovis, Mina and Gao, *IEEE Aerospace Conf. 2024*

The Near-Term Lunar Landscape



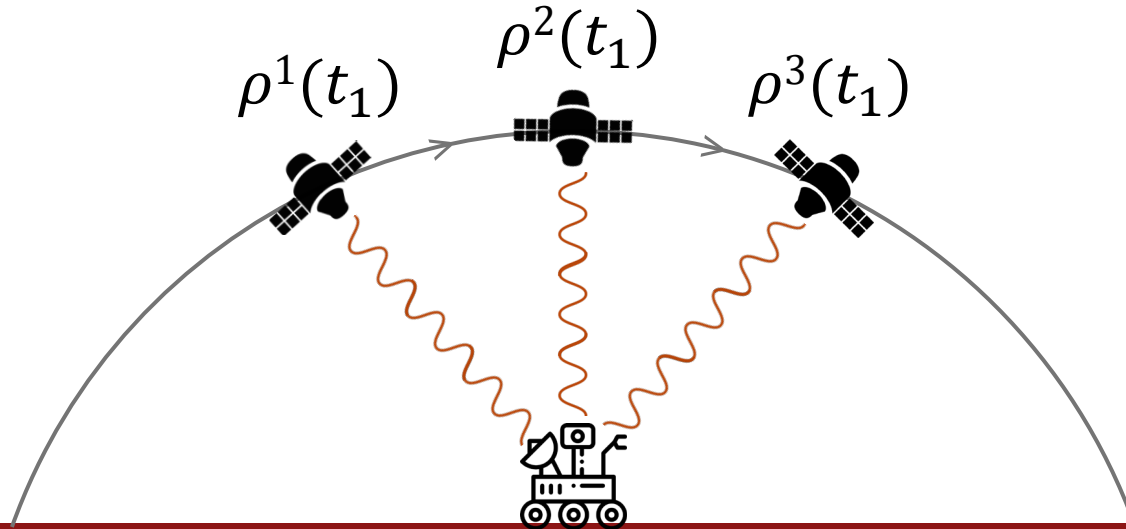
Lunar Pathfinder Satellite

- Data Relay Satellite
- in elliptical lunar frozen orbit (ELFO)
- *Service: ~2025 - 2033*



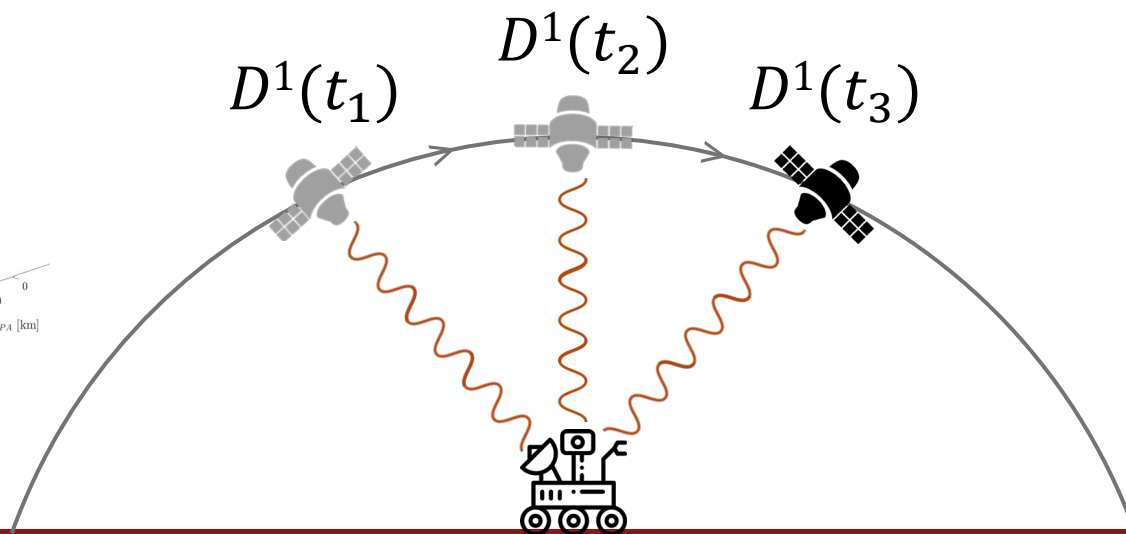
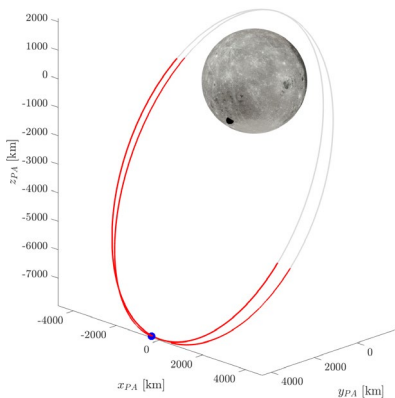
Desired Scenario with LunaNet

- **Multiple satellites** – instantaneous localization (with at least 4 satellites)
- **Navigation payload** – obtain pseudorange measurements for trilateration



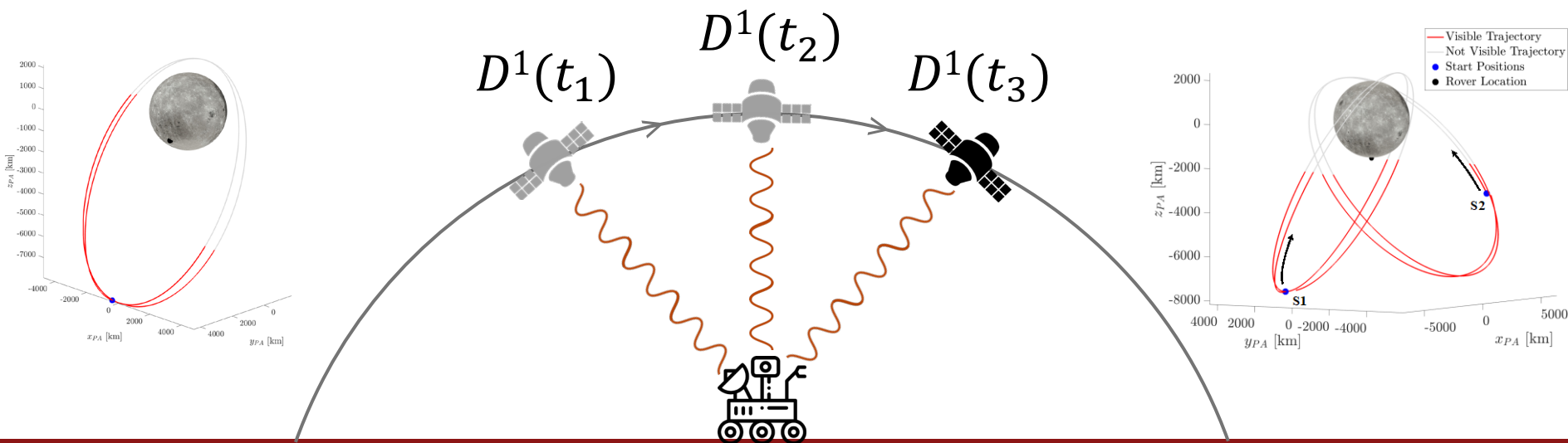
Current Scenario

- *Single satellite*
- *No navigation payload*

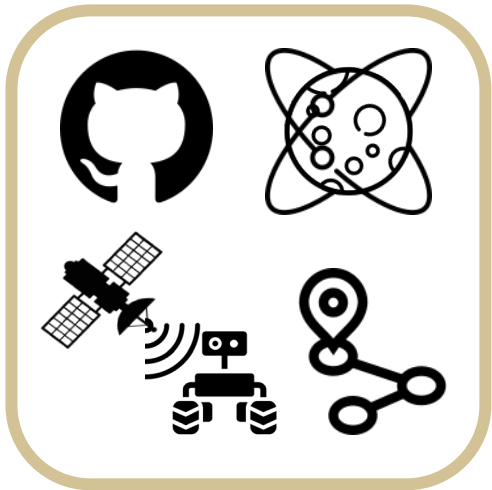


Key Ideas

- **Single satellite** – measurements over time -> multiple virtual satellites
- **No navigation payload** – use Doppler shift observables
- **Adding a second satellite** – Benefits and optimal SV placement

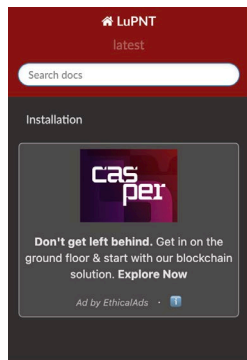


6. LuPNT: an Open-Source Simulator



- Casadesus Vila, Iiyama and Gao, IEEE Aerospace Conf. 2025
- Casadesus Vila, Iiyama and Gao, ION GNSS+ 2023

Open-Source *LuPNT* Simulator



🏠 / Welcome to the LuPNT Library

Welcome to the LuPNT Library

LuPNT is an open-source C++/Python library for Lunar Positioning (LuPNT).

Note

This project is under active development

Attribution

This project is a product of the [Stanford NAV Lab](#). If using this the following:

Module	# files	# lines
 lupnt	75	10,800
 pylupnt	25	3,200
 projects	85	19,300
 test	20	1,200
Total	215	35,300

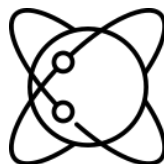
~600 pages



Open-source
simulator for lunar
PNT services



GNSS measurement
modeling
at lunar region



Astrodynamics
with automatic
differentiation



Satellite-to-satellite
measurements and
communication

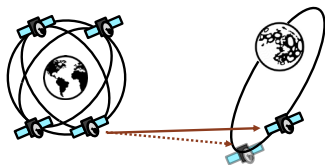


Modular and extensible
to multiple research
purposes

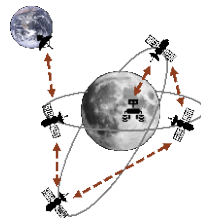
Summary of Our Research Efforts on Designing Lunar Navigation Satellite Systems



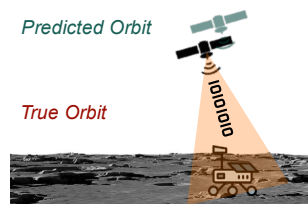
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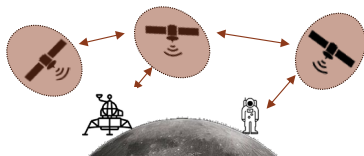
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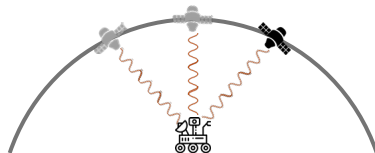
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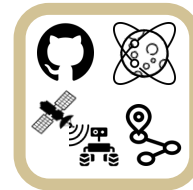
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5. Intermediate step with 1-2 satellites



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Thank You!

